

$$F(s) = \frac{s^2 + 2s + 1}{(s+3)^3 \cdot s^2}$$

$$F(s) = \frac{A_1}{(s+3)} + \frac{A_2}{(s+3)^2} + \frac{A_3}{(s+3)^3} + \frac{B_1}{s} + \frac{B_2}{s^2}$$

$$f(t) = A_1 \cdot e^{-3t} + A_2 \cdot t \cdot e^{-3t} + A_3 \cdot \frac{1}{2} \cdot t^2 \cdot e^{-3t} + B_1 \cdot 1(t) + B_2 \cdot t$$

$$A_3 = \left. \frac{(s^2 + 2s + 1) \cdot (s+3)^3}{(s+3)^3 \cdot s^2} \right|_{s=-3} = \frac{(-3)^2 + 2 \cdot (-3) + 1}{(-3)^2} = \frac{9 - 6 + 1}{9} = \frac{4}{9}$$

$$A_2 = \frac{1}{1!} \cdot \frac{d}{ds} \left( \frac{s^2 + 2s + 1}{s^2} \right) \Big|_{s=-3} = (2s+2) \cdot s^{-2} - 2 \cdot s^{-3} \cdot (s^2 + 2s + 1) \Big|_{s=-3} = \frac{2 \cdot (-3) + 2}{(-3)^2} - 2 \cdot \frac{(-3)^2 + 2 \cdot (-3) + 1}{(-3)^3}$$

$$= -\frac{4}{9} - 2 \cdot \frac{9 - 6 + 1}{(-27)} = -\frac{4}{9} + \frac{2 \cdot 4}{27} = -\frac{12}{27} + \frac{8}{27} = -\frac{4}{27}$$

$$A_1 = \frac{1}{2!} \cdot \frac{d}{ds} \left( \left[ (2s+2) \cdot s^{-2} - 2 \cdot s^{-3} \cdot (s^2 + 2s + 1) \right] \right) \Big|_{s=-3} = \left[ 2 \cdot s^{-2} - 2 \cdot s^{-3} \cdot (2s+2) \right] - 2 \left[ (2s+2) \cdot s^{-3} - 3 \cdot s^{-4} \cdot (s^2 + 2s + 1) \right] \Big|_{s=-3}$$

$$= \frac{1}{2} \cdot \left[ \frac{2}{(-3)^2} - \frac{2}{(-3)^3} \cdot (2 \cdot (-3) + 2) \right] - 2 \cdot \left[ (2 \cdot (-3) + 2) \cdot \frac{1}{(-3)^3} - 3 \cdot \frac{1}{(-3)^4} \cdot ((-3)^2 + 2 \cdot (-3) + 1) \right] =$$

$$= \frac{1}{2} \cdot \left[ \frac{2}{9} + \frac{2 \cdot (-4)}{27} - 2 \cdot \left( \frac{4}{27} - \frac{3 \cdot (9 - 6 + 1)}{81} \right) \right] - \frac{1}{2} \cdot \left[ \frac{2}{9} - \frac{8}{27} - \frac{8}{27} + \frac{24}{81} \right] =$$

$$= \frac{1}{2} \cdot \left[ \frac{6}{27} - \frac{8}{27} - \frac{8}{27} + \frac{8}{27} \right] = \frac{1}{2} \cdot \left( -\frac{2}{27} \right) = -\frac{1}{27}$$

$$B_2 = \left. \frac{(s^2 + 2s + 1) \cdot s^2}{(s+3)^3 \cdot s^2} \right|_{s=0} = \frac{0^2 + 2 \cdot 0 + 1}{(0+3)^3} = \frac{1}{27}$$

$$B_1 = \frac{1}{1!} \cdot \frac{d}{ds} \left[ (s^2 + 2s + 1) \cdot (s+3)^{-3} \right] \Big|_{s=0} = \left[ (2s+2) \cdot (s+3)^{-3} - 3 \cdot (s+3)^{-4} \cdot 1 \cdot (s^2 + 2s + 1) \right] \Big|_{s=0}$$

$$= \frac{2 \cdot 0 + 2}{(0+3)^3} - \frac{3 \cdot 1 \cdot (0^2 + 2 \cdot 0 + 1)}{(0+3)^4} = \frac{2}{27} - \frac{3}{81} = \frac{2}{27} - \frac{1}{27} = \frac{1}{27}$$

$$f(t) = -\frac{1}{27} \cdot e^{-3t} - \frac{4}{27} \cdot t \cdot e^{-3t} + \frac{2}{9} \cdot t^2 \cdot e^{-3t} + \frac{1}{27} \cdot 1(t) + \frac{1}{27} \cdot t$$