

## Set of derivatives of basic functions

$$\frac{df(x)}{dx} = f'(x) = \dot{f}(x)$$

$$C' = 0; \text{ where } C - \text{constant}$$

$$(x^p)' = p \cdot x^{p-1}; \text{ where } p \in \mathbb{R}$$

$$(\sqrt[n]{x})' = \frac{1}{n \cdot \sqrt[n]{x^{n-1}}}$$

$$(\sin x)' = \cos x$$

$$(\cos x)' = -\sin x$$

$$\tan x = \frac{1}{\cos^2 x}$$

$$(\cot x)' = \frac{-1}{\sin^2 x}$$

$$(e^x)' = e^x$$

$$(a^x)' = a^x \cdot \ln a$$

$$(\ln x)' = \frac{1}{x}$$

$$(\log_a x)' = \frac{1}{x \cdot \ln a}$$

$$(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$$

$$(\arccos x)' = \frac{-1}{\sqrt{1-x^2}}$$

$$(\arctan x)' = \frac{1}{x^2 + 1}$$

$$(\operatorname{arccot} x)' = \frac{-1}{x^2 + 1}$$

In geometric interpretation function's derivative is tangent of angle ( $\tan \alpha$ ) by which tangent is inclined relative to the function.

## Basic theorems for derivatives

If functions  $f(x)$  and  $g(x)$  are differentiable then functions  $c \cdot f(x)$  ( $c$  – constant),  $f(x) + g(x)$ ,  $f(x) - g(x)$ ,  $f(x) \cdot g(x)$ ,  $\frac{f(x)}{g(x)}$  {for points where  $g(x) \neq 0$ } are also differentiable.

Moreover:

$$(c \cdot f(x))' = c \cdot f'(x)$$

$$(f(x) \mp g(x))' = f'(x) \mp g'(x)$$

$$(f(x) \cdot g(x))' = f'(x) \cdot g(x) + f(x) \cdot g'(x)$$

$$\left(\frac{f(x)}{g(x)}\right)' = \frac{f'(x) \cdot g(x) - f(x) \cdot g'(x)}{g^2(x)}$$

## Theorems about derivative of complex function

Function  $g(x)$  over function  $f(x)$ .

$$(g(x) \circ f(x))' = g'(x) \cdot f(x) \cdot f'(x)$$