



$$E_{k1} = 0$$

$$E_{k2} = \frac{I_2 \omega^2}{2}$$

$$v = \omega \cdot l$$

$$\omega = \frac{v}{l}$$

Known:

$m$  - mass of rod [kg]

$l$  - length of rod [m]

$g$  - gravity acceleration [ $m/s^2$ ]

Find:

final velocity  $v_k$  of rod point B, when rod will be in horizontal position

$$E_{p1} + E_{k1} = E_{p2} + E_{k2}$$

$I_0 = \frac{1}{12} ml^2$  moment of inertia for rod, when rotational axis is in the rod's center

Parallel axis theorem,  $d$  is a distance between axes

$$I_2 = I_0 + md^2$$

$$I_2 = \frac{1}{12} ml^2 + m \cdot \left(\frac{l}{2}\right)^2$$

$$I_2 = \frac{1}{12} ml^2 + \frac{1}{4} ml^2$$

$$I_2 = \frac{1}{3} ml^2$$

$$E_{p1} = E_{k2}$$

$$\frac{1}{2} mgl = \frac{I_2 \omega^2}{2} \quad | \cdot 2$$

$$m \cdot g \cdot l = I_2 \cdot \omega^2$$

$$m \cdot g \cdot l = \frac{1}{3} m \cdot l^2 \cdot \left(\frac{v_k}{l}\right)^2$$

$$m \cdot g \cdot l = \frac{1}{3} m \cdot l^2 \cdot \frac{v_k^2}{l^2} \quad | \cdot m \quad | \cdot 3$$

$$3 \cdot g \cdot l = v_k^2$$

$$v_k = \sqrt{3 \cdot g \cdot l}$$